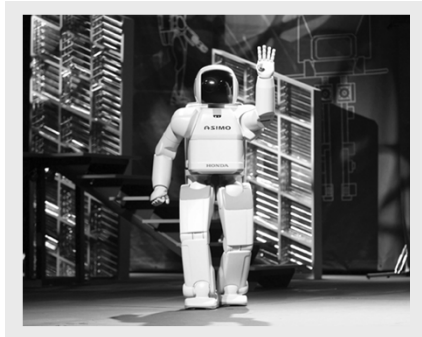


Humanoid Robots

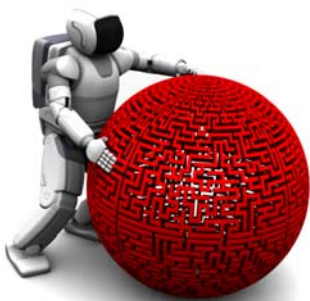
The Challenge:
beyond mobility



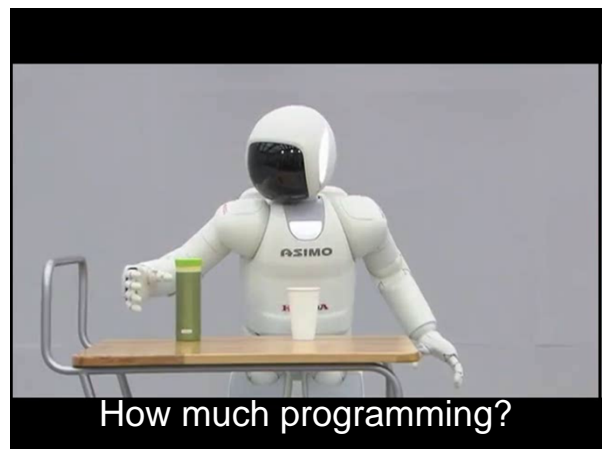
.. not only walk, but also interact with the world!
a unified mobility & manipulation framework!



ASIMO



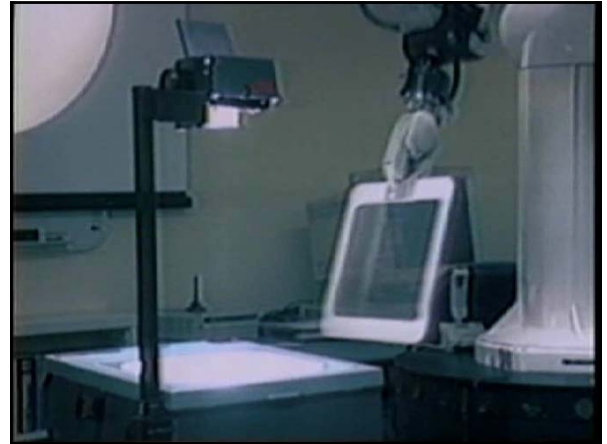
.. not only walk, but also interact with the world!



How much programming?

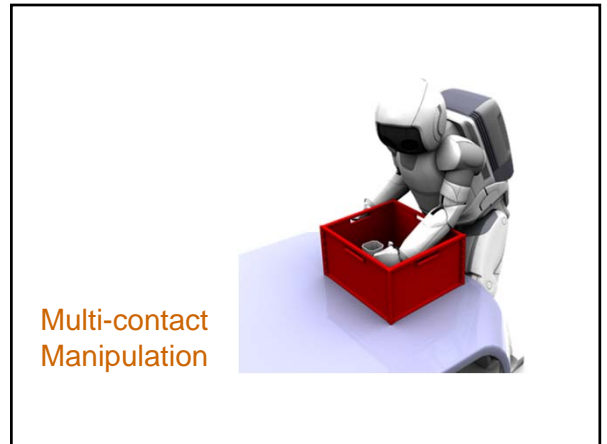
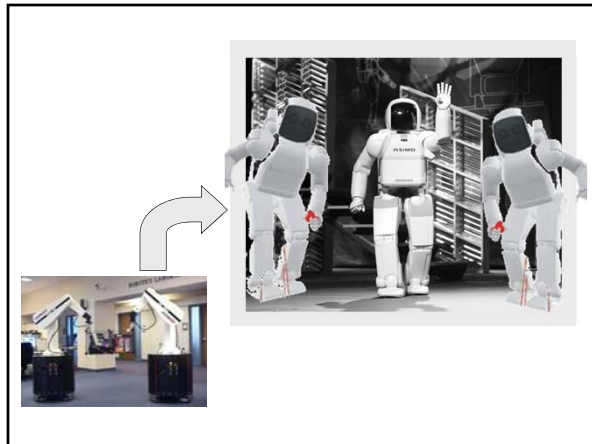
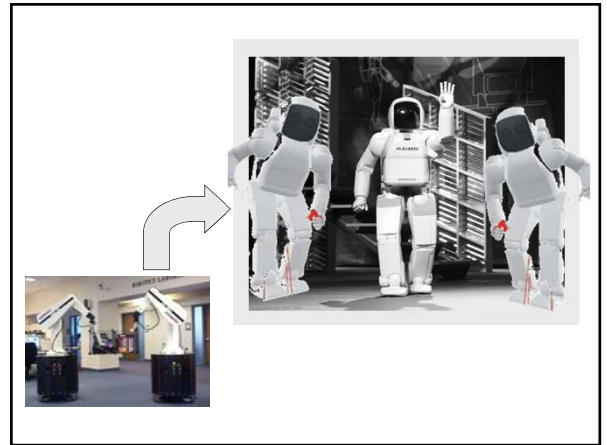
Mobile Manipulation

Human Guided Motion & Human-Robot Interaction
Romeo & Juliet (1993)



Human-Robot Interaction

Romeo & Juliet (1993-96)



Humanoid Robot Control

branching and under-actuated

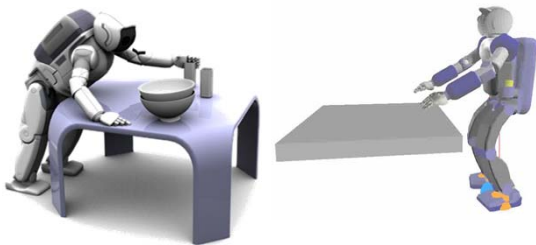
- whole-body control
- constraints and obstacles
- multiple contacts
- internal forces & balance
- manipulation skills



Multi-Contact Whole Body Motion



Physical Interaction, Constraints, and Task Behaviors



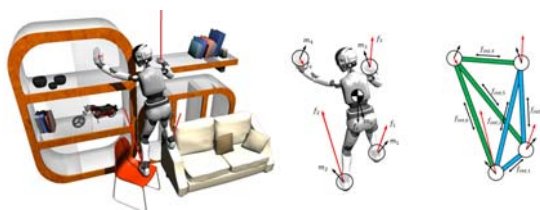
Balanced Supporting Contacts

Internal Force Control – Virtual Linkage



Balanced Supporting Contacts

Internal Force Control – Virtual Linkage



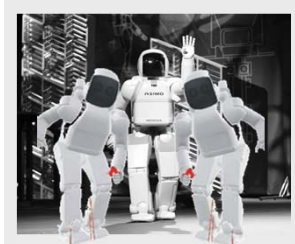
Physical Interaction, Constraints, and Task Behaviors



Posture
Task Behavior
Multiple Contacts
Internal Constraints
Self Collision
Local Obstacles
Balance

Unified Whole-Body Control Framework

posture
consistent with {
 Task
consistent with {
 contact
consistent with {
 internal constraints
 self collision
 local obstacles
consistent with {
 balance



interact with the world,
 cooperate, and manipulate

} } } }

Constraint-Consistent Task-Space

$$v_{\otimes} \in cc - space$$



interact with the world,
 cooperate, and manipulate

Unified Whole Body Control Framework

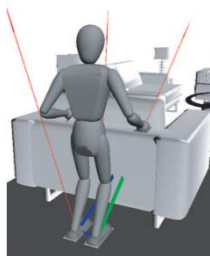
Task, Posture, Constraints, Multiple Contacts, and Balance

Dynamics

$$\Lambda_{\otimes} \dot{g}_{\otimes} + \mu_{\otimes} + p_{\otimes} + F_f = F_{\otimes}$$

Control

$$F_{\otimes} = \hat{\Lambda}_{\otimes} F_{\otimes}^* + \hat{\mu}_{\otimes} + \hat{p}_{\otimes}$$



Whole-body Control



Task & Posture Decomposition

Task Dynamics and Control

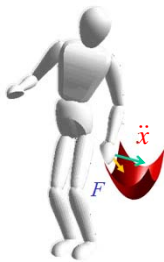
Task Dynamics

$$\Lambda \ddot{x} + \mu + p = F$$

Task Control

$$H = \hat{\Lambda} (-\nabla V_{Task}) + \hat{\mu} + \hat{p}$$

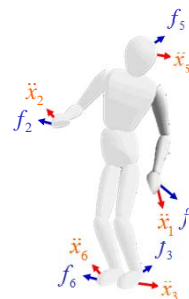
$$\Gamma = J^T F$$



Task Dynamics – Branching Structures

$$x = \begin{pmatrix} x_1 \\ x_2 \\ \vdots \\ x_m \end{pmatrix} \quad \Lambda = \begin{pmatrix} \Lambda_{11} & \Lambda_{12} & \dots & \Lambda_{1L} \\ \Lambda_{21} & \Lambda_{22} & \dots & \Lambda_{2L} \\ \dots & \dots & \dots & \dots \\ \Lambda_{L1} & \Lambda_{L2} & \dots & \Lambda_{LL} \end{pmatrix} \quad x \Rightarrow J \Rightarrow \Lambda$$

$$\Lambda \ddot{x} + \mu + p = F$$



Posture Space Control

Joint-Space Dynamics


Posture

Task-related

$= \Gamma$

$$\Lambda \ddot{x} + \mu + p = F$$

$\bar{J}^T \downarrow$
 $\uparrow J^T$



$N^T \downarrow$

Task Control: J^T

Posture Control: N^T

Control Structure



$$\Gamma = J_{task}^T F_{task} + N_{task}^T \Gamma_{posture}$$

Decomposition of torque vector

Dynamic Consistency

⇒

$\ddot{x}_{task} = 0$

Posture Energy

Whole-Body Control: Dynamics

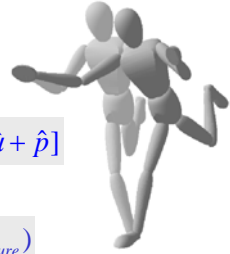
$$\Gamma = \Gamma_{Task} + \Gamma_{Posture}$$

$$\Gamma_{Task} = J^T F$$

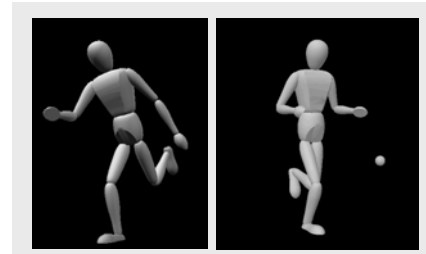
$$\Gamma_{Task} = J^T [\hat{\Lambda} (-\nabla V_{Task}) + \hat{\mu} + \hat{p}]$$

$$\Gamma_{Posture} = N^T \Gamma_{Desired-Posture}$$

$$\Gamma_{Posture} = N^T (-\nabla V_{Desired-Posture})$$



Dynamics in Posture Space



Posture Dynamics & Control

Posture sub-task: $x_p \rightarrow J_p$

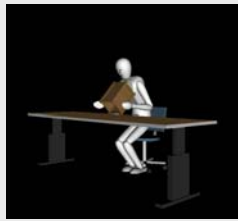
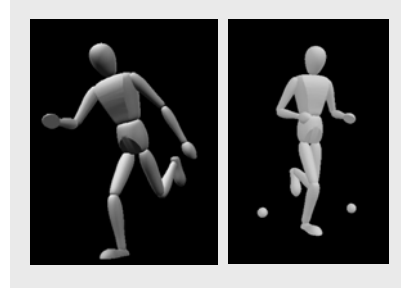
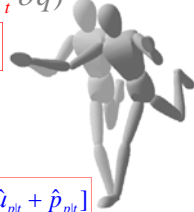
Task-consistent posture Jacobian: $\delta x_{plt} = J_p (N_t \delta q)$

Dynamics: $J_{plt} = J_p N_t$

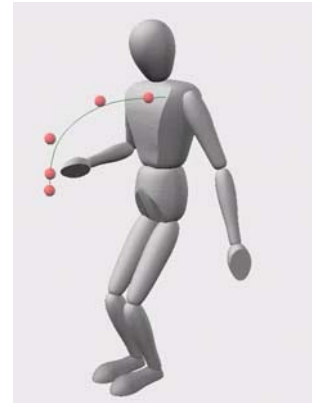
$$\Lambda_{plt} \ddot{x}_{plt} + \mu_{plt} + p_{plt} = F_{plt}$$

Control:

$$\Gamma_{posture} = J_{plt}^T [\hat{\Lambda}_{plt} (-\nabla V_{posture}) + \hat{\mu}_{plt} + \hat{p}_{plt}]$$

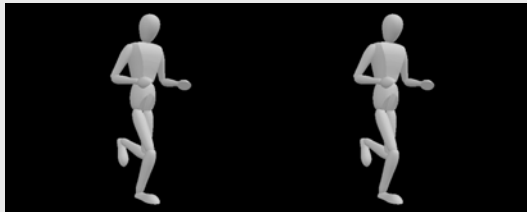


Constraints

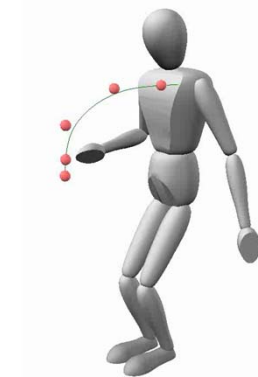


Self Collision

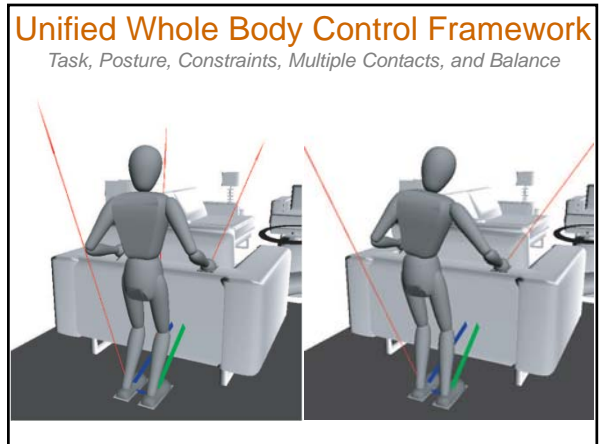
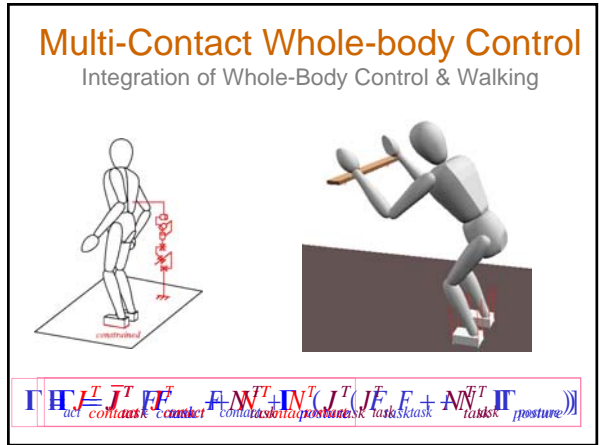
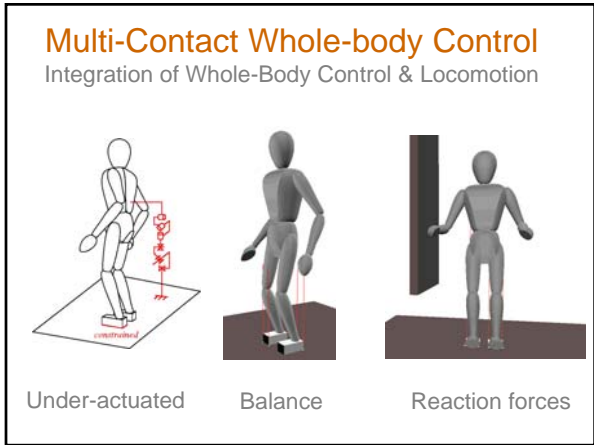
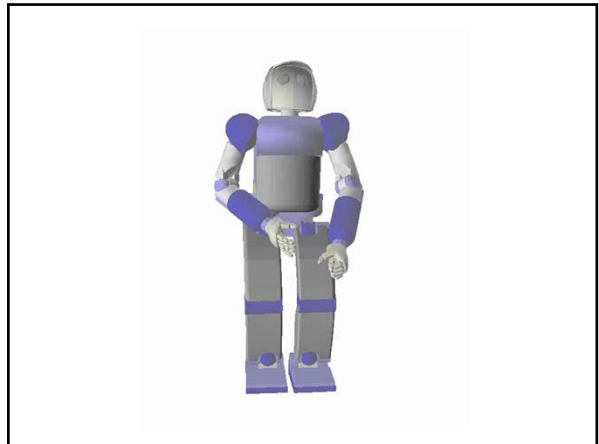
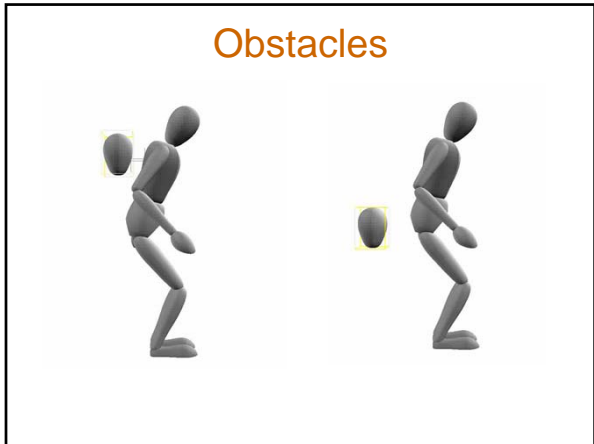
Constraints and Priorities



$$\Gamma = J_{task}^T F_{task} + N_{task}^T (\Gamma_{task} + N_{posture}^T \Gamma_{posture})$$

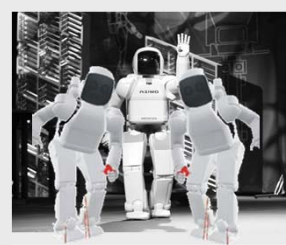


Self Collision



Unified Framework

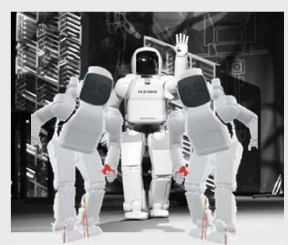
posture
consistent with {
 task
consistent with {
 contact
consistent with {
 internal constraints
 self collision
 local obstacles
consistent with {
 balance
 } } } }



interact with the world,
cooperate, and manipulate


Constraint-Consistent Task-Space

$v_{\otimes} \in cc - space$



interact with the world,
cooperate, and manipulate

Constraint-Consistent Task-Space

$$v_{\otimes} = \begin{pmatrix} v_{c|s} \\ v_{f|c|s} \\ v_{m|f|c|s} \\ v_{p|m|f|c|s} \end{pmatrix}$$


interact with the world,
cooperate, and manipulate

Unified Whole Body Control Framework

Task, Posture, Constraints, Multiple Contacts, and Balance

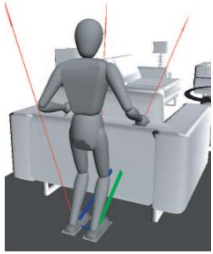
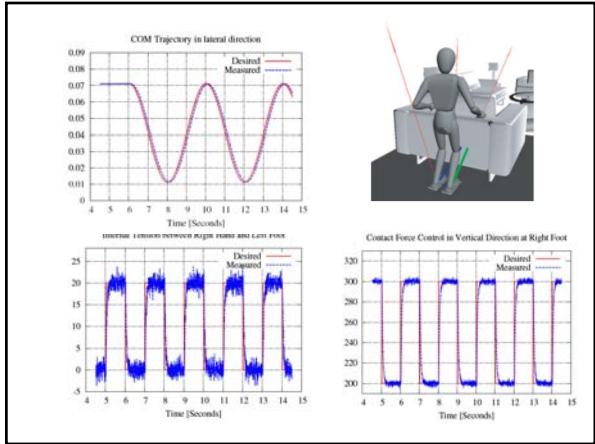
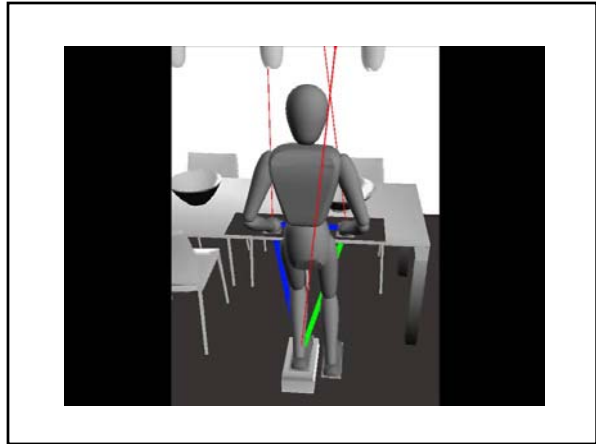
Dynamics

$$\Lambda_{\otimes} \dot{\xi}_{\otimes} + \mu_{\otimes} + p_{\otimes} + F_f = F_{\otimes}$$

Control

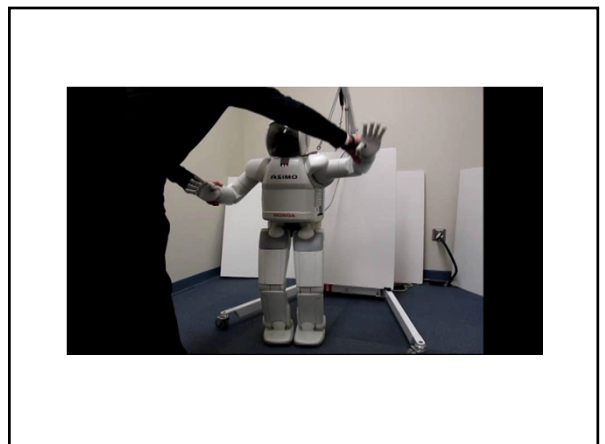
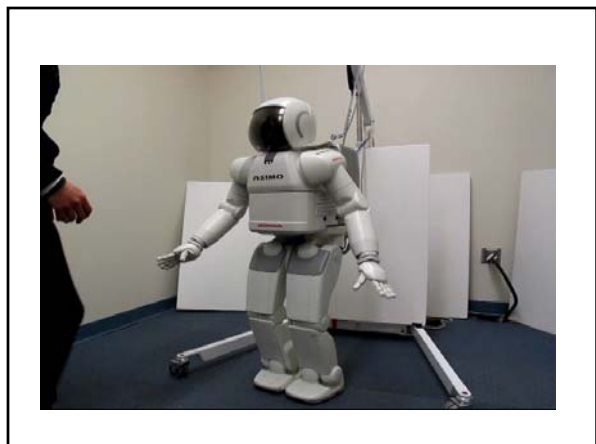
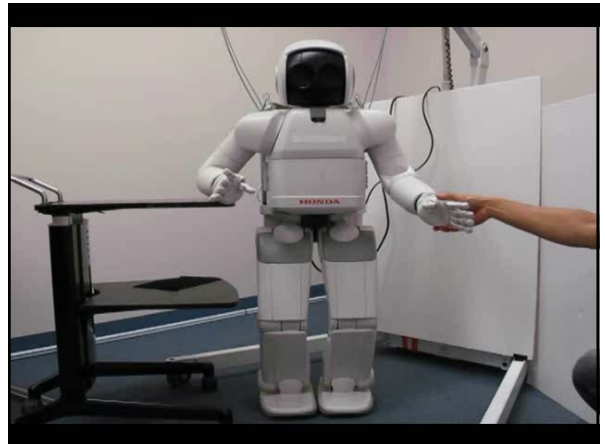
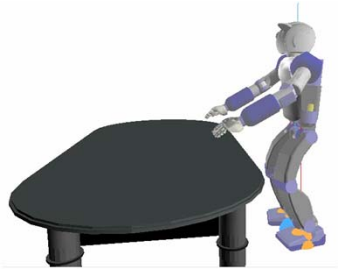
$$F_{\otimes} = \hat{\Lambda}_{\otimes} F_{\otimes}^* + \hat{\mu}_{\otimes} + \hat{p}_{\otimes}$$

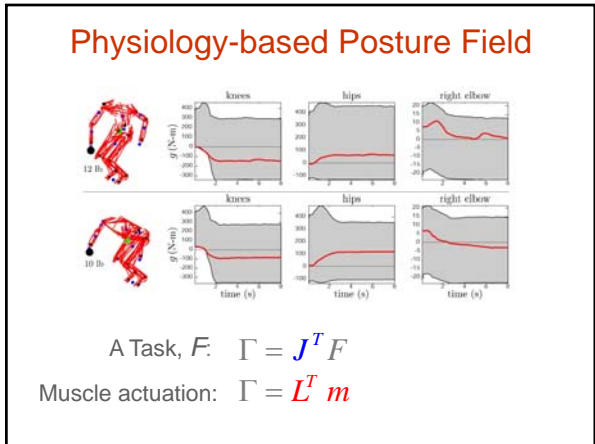
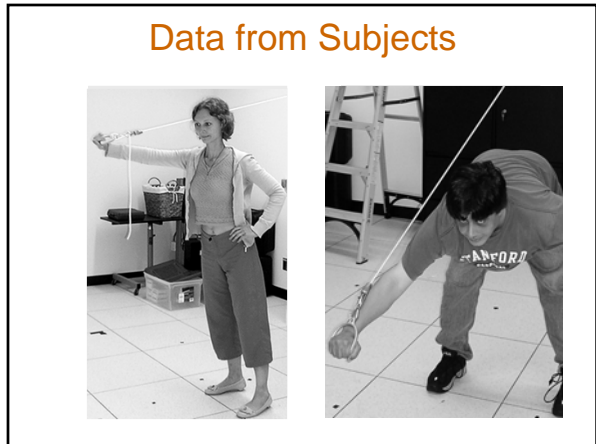
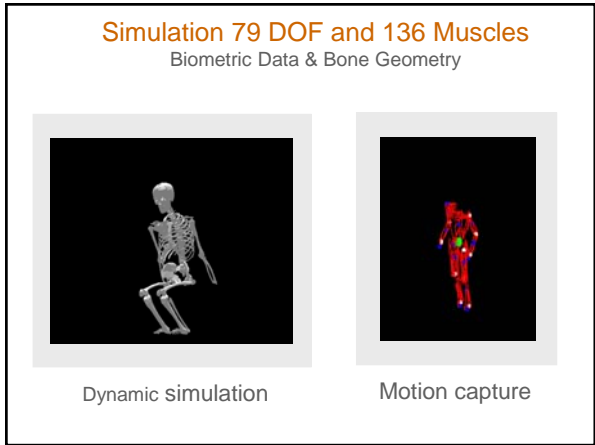
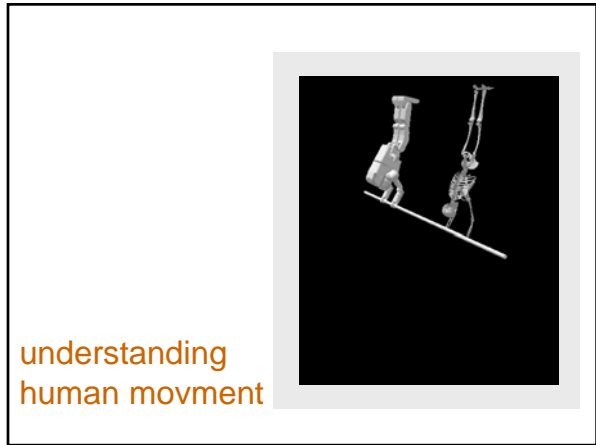
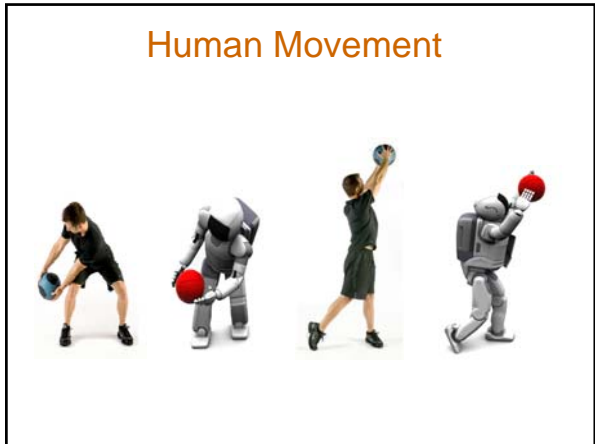
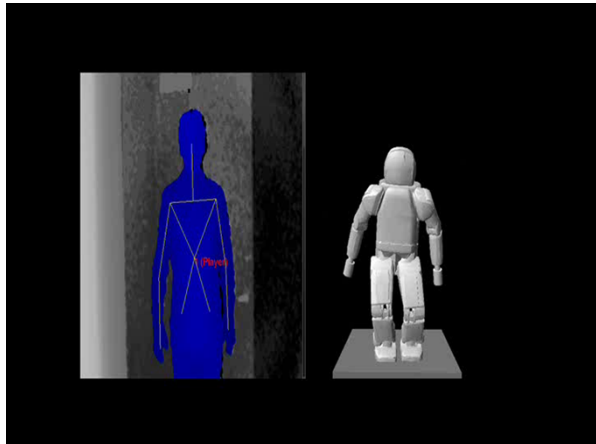
Actuated Torques

$$\Gamma_a = (\overline{UN}_s)^T J_{\otimes}^T F_{\otimes}$$



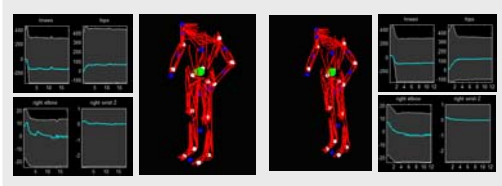
Unified Whole Body Control Framework

Task, Posture, Constraints, Multiple Contacts, and Balance





Data from Subjects



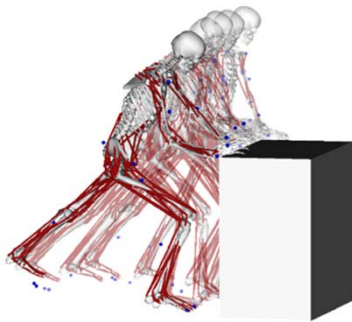
Learning from the Human

Humans grow to learn the efficiency of the body's *physio-mechanical advantage*

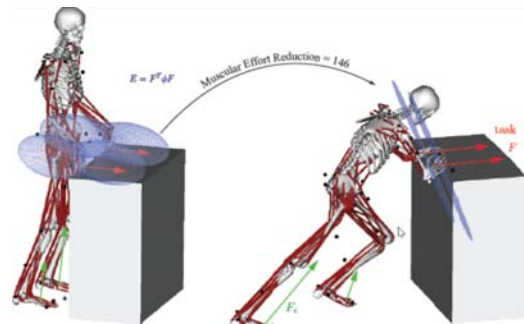
In learned tasks, humans minimize muscular effort, under physical and "social" constraints



Physio-Mechanical Advantage



Physio-Mechanical Advantage



Physiology-based Posture Field

Human posture is continuously adjusted to reduce muscular effort

Muscular Energy minimization:

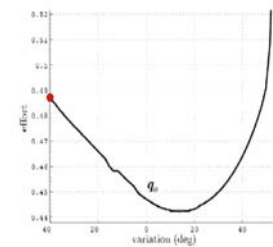
$$E = cm^2$$

Function of physiology, mechanical advantage, and task

$$E = F^T [J(L^T N_c^{-2} L)^{-1} J^T] F \quad E = F^T \Phi F$$

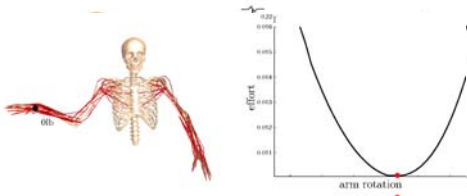


Validation - Arm Effort



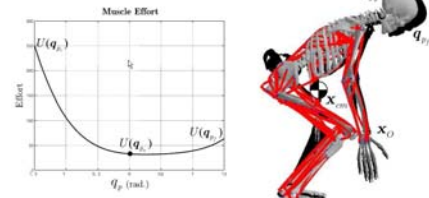
$$E = cm^2$$

Validation - Arm Effort



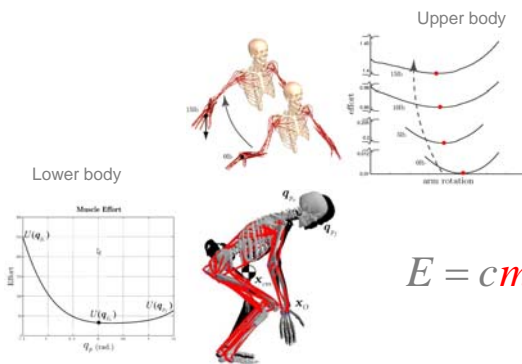
$$E = cm^2$$

Validation – whole-body effort

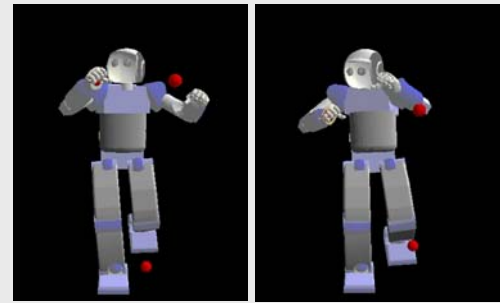


$$E = cm^2$$

Physio-Mechanical Advantage



$$E = cm^2$$



ASIMO

SAI Neuromuscular Library

